# Mathletics <br> Victorian Program of Studies 

## Skill Quests



Years 9-10
Mathletics
May, 2022

## Mathletics

Victoria Program of Studies
Skill Quests
May 2022
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## Year 9

## 1 Number and Algebra

### 1.1 Real numbers

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 1. Solve problems involving direct proportion. Explore the relationship between graphs and equations corresponding to simple rate problems | Proportion, rates, graphs \& equations | Unit rates |
|  |  | Converting rates |
|  |  | Direct proportion |
|  |  | Indirect/inverse proportion |
|  |  | Direct \& inversely proportionate graphs |
|  |  | Interpreting \& using conversion graphs |
|  |  | The constant of proportionality |
|  |  | Graphing equations of direct proportion |
|  |  | Solving distance, speed \& time problems |
|  |  | Travel graphs |
| 2. Apply index laws to numerical expressions with integer indices | Index laws with numerical expressions | Mixed index laws numerical expressions |
|  |  | Index laws: positive \& negative integer index |
| 3. Express numbers in scientific notation | Express numbers in scientific notation | Introducing scientific notation |
|  |  | Converting scientific notation \& basic numbers |
|  |  | Calculating \& rounding with scientific notation |

### 1.2 Money and financial mathematics

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 4. Solve problems involving simple <br> interest | Solve problems <br> involving simple <br> interest | Simple interest <br> Understanding hire purchase <br> agreements |

### 1.3 Patterns and algebra

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 5. Extend and apply the index laws <br> to variables, using positive integer <br> indices and the zero index | Index laws with <br> variables | Mixed index laws algebraic <br> expressions |


| 6. Apply the distributive law to the <br> expansion of algebraic expressions, <br> including binomials, and collect like <br> terms where appropriate | Applying the <br> distributive law | Applying the distributive law |
| :--- | :--- | :--- |

### 1.4 Linear and non-linear relationships

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 8. Find the distance between two <br> points located on the Cartesian <br> plane using a range of strategies, <br> including graphing software | Find the distance <br> between two points | Distance between two points <br> without the formula |
| 9. Find the midpoint and gradient of <br> a line segment (interval) on the <br> Cartesian plane using a range of <br> strategies, including graphing <br> software | Midpoint \& gradient of <br> line segments | Distance between two points <br> using the formula |

## 2 Measurement and Geometry

### 2.1 Using units of measurement

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 2. Calculate areas of composite shapes | Areas of composite shapes | Areas of composite shapes |
| 3. Calculate the surface area and volume of cylinders and solve related problems | Surface area \& volume of cylinders | Volumes of cylinders |
|  |  | Surface area of cylinders |
| 4. Solve problems involving the surface area and volume of right prisms | Surface area \& volume of right prisms | Surface area of right prisms with nets |
|  |  | Finding surface area problems |
|  |  | Volumes of composite right prisms |
| 5. Investigate very small and very large time scales and intervals | Lge/sml amounts of time, data \& limits | Significant figures |
|  |  | Amounts of data |
|  |  | Large \& small time intervals |
|  |  | Representing large \& small numbers |
|  |  | Limits of accuracy |

### 2.2 Geometric reasoning

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 6. Use the enlargement <br> transformation to explain similarity <br> and develop the conditions for <br> triangles to be similar | Similar triangles | Introducing similarity |
|  |  | Similar triangles |
| 7. Solve problems using ratio and <br> scale factors in similar figures | Scale factors with <br> similar figures | Scale factors |
|  | Area \& volume scale factors |  |

### 2.3 Pythagoras and trigonometry

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 8. Investigate Pythagoras' theorem <br> and its application to solving simple <br> problems involving right angled <br> triangles | Pythagoras' theorem | Identifying sides on right- <br> angled triangles |
|  |  | Finding a shorter side using <br> Pythagoras' theorem |


|  |  | Finding the hypotenuse using <br> Pythagoras' theorem |
| :--- | :--- | :--- |
|  | Solving problems involving <br> Pythagoras' theorem |  |
|  | Exploring Pythagorean triads <br> Using the converse of <br> Pythagoras' theorem |  |
|  | Solving Pythagoras' theorem <br> problems: exact values |  |
| 9. Use similarity to investigate the <br> constancy of the sine, cosine and <br> tangent ratios for a given angle in <br> right-angled triangles | Introduction to <br> trigonometry | Introducing trigonometry |
| 10. Apply trigonometry to solve <br> right-angled triangle problems | Apply trigonometry | Finding the missing side using <br> rigig ratios |
| tringles |  |  |

## 3 Statistics and Probability

### 3.1 Chance

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 1. List all outcomes for two-step chance experiments, both with and without replacement using tree diagrams or arrays. Assign probabilities to outcomes and determine probabilities for events | List outcomes \& find probabilities | The fundamental counting principle |
|  |  | Two-step chance experiments with replacement |
|  |  | Two-step chance experiments without replacement |
| 2. Calculate relative frequencies from given or collected data to estimate probabilities of events involving 'and' or 'or' | Calculate \& use relative frequency | Calculating \& using relative frequency |
| 3. Investigate reports of surveys in digital media and elsewhere for information on how data were obtained to estimate population means and medians | Make population predictions from data | Using data to make predictions about populations |

### 3.2 Data representation and interpretation

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 4. Identify everyday questions and <br> issues involving at least one <br> numerical and at least one <br> categorical variable, and collect <br> data directly and from secondary <br> sources | Collect everyday data | Collecting everyday data |
| 5. Construct back-to-back stem- <br> and-leaf plots and histograms and <br> describe data, using terms including <br> 'skewed', 'symmetric' and 'bi modal' | Construct \& interpret <br> data displays | Constructing \& interpreting <br> data displays |
| 6. Compare data displays using <br> mean, median and range to <br> describe and interpret numerical <br> data sets in terms of location <br> (centre) and spread | Compare data displays | Comparing data displays |

## Year 10

## 1 Number and Algebra

### 1.1 Money and financial mathematics

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 8. Connect the compound interest <br> formula to repeated applications of <br> simple interest using appropriate <br> digital technologies | Compound \& simple <br> interest | Compound interest |

### 1.2 Patterns and algebra

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 9. Factorise algebraic expressions by taking out a common algebraic factor | Factorise algebraic expressions | Factorising algebraic expressions |
| 10. Simplify algebraic products and quotients using index laws | Index laws | Indices: Multiplication |
|  |  | Indices: Division |
|  |  | Indices: Power of a power |
|  |  | Indices: Zero index |
|  |  | Indices: Mixed basic operations with coefficient = 1 |
|  |  | Indices: Mixed basic operations with coefficient >1 |
|  |  | Indices: Negative index with numerical base |
|  |  | Indices: Negative index, algebraic \& numerical base |
|  |  | Indices: Mixed with negative indices |
| 11. Apply the four operations to simple algebraic fractions with numerical denominators | Algebraic fractions | Algebraic fractions: 4 ops numerical denominators |
|  |  | Algebraic fractions: Simplifying |
| 12. Expand binomial products and factorise monic quadratic expressions using a variety of strategies | Binomial expansions \& basic quadratics | Expanding binomial products |
|  |  | Binomial product special results |
|  |  | Factorising monic quadratic trinomials |
|  |  | Further binomial expansions |
| 13. Substitute values into formulas to determine an unknown and rearrange formulas to solve for a particular term | Substitute into formulas | Using authentic formula |

### 1.3 Linear and non-linear relationships

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 15. Solve problems involving linear equations, including those derived from formulas | Problems involving linear equations | Word problems |
| 16. Solve linear inequalities and graph their solutions on a number line | Linear inequalities \& their graphs | Understanding inequalities |
|  |  | Solving linear inequalities |
| 17. Solve linear simultaneous equations, using algebraic and graphical techniques, including using digital technology | Linear simultaneous equations | Simultaneous equations |
| 18. Solve problems involving parallel and perpendicular lines | Parallel \& perpendicular lines | Parallel lines |
|  |  | Perpendicular lines |
|  |  | Equations of lines: Parallel \& perpendicular lines |
|  |  | Problems involving parallel \& perpendicular lines |
| 19. Explore the connection between algebraic and graphical representations of relations such as simple quadratics, circles and exponentials using digital technology as appropriate | Representations of non-linear relations | Graphing representations of non-linear relations |
| 20. Solve linear equations involving simple algebraic fractions | Equations involving algebraic fractions | Solving equations involving algebraic fractions |
| 21. Solve simple quadratic equations using a range of strategies | Solve simple quadratic equations | Solving simple quadratic equations |

## 2 Measurement and Geometry

### 2.1 Using units of measurement

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 3. Solve problems involving surface <br> area and volume for a range of <br> prisms, cylinders and composite <br> solids | Area of volume of <br> composite solids | Surface area of composite <br> solids |
|  |  | Volume of composite solids |

### 2.2 Geometric reasoning

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 5. Apply logical reasoning, including <br> the use of congruence and <br> similarity, to proofs and numerical <br> exercises involving plane shapes | Solve problems using <br> geometric reasoning | Solving problems using <br> geometric reasoning |

### 2.3 Pythagoras and trigonometry

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 6. Solve right-angled triangle <br> problems including those involving <br> direction and angles of elevation <br> and depression |  <br> depression |  <br> depression |
|  | Bearings | Compass bearings |
|  |  | True bearings |

## 3 Statistics and Probability

### 3.1 Chance

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 7. Describe the results of two- and three-step chance experiments, both with and without replacements, assign probabilities to outcomes and determine probabilities of events. Investigate the concept of independence | Two/three step experiments, independence | Three-step chance experiments with replacement |
|  |  | Three-step chance experiments without replacement |
|  |  | Independent events |
| 8. Use the language of 'if....then, 'given', 'of', 'knowing that' to investigate conditional statements and identify common mistakes in interpreting such language | Conditional probability | Conditional probability introduction |
|  |  | Conditional probability \& twoway tables |
|  |  | Conditional probability \& tree diagrams |
|  |  | Conditional probability \& arrays |
|  |  | Conditional probability \& Venn diagrams |
|  |  | Set theory \& Venn diagrams |

### 3.2 Data representation and interpretation

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 9. Determine quartiles and <br> interquartile range and investigate <br> the effect of individual data values, <br> including outliers on the <br> interquartile range | Interquartile range | Interquartile range |
| 10. Construct and interpret box <br> plots and use them to compare <br> data sets | Construct \& interpret <br> box plots | Constructing \& interpreting <br> box plots |
| 11. Compare shapes of box plots to <br> corresponding histograms and dot <br> plots and discuss the distribution of <br> data | Compare box plots | Comparing box plots |
| 12. Use scatter plots to investigate <br> and comment on relationships <br> between two numerical variables | Scatter plots | Scatter plots |
| 13. Investigate and describe <br> bivariate numerical data where the <br> independent variable is time | Bivariate data | Bivariate data |
| 14. Evaluate statistical reports in <br> the media and other places by <br> linking claims to displays, statistics <br> and representative data | Evaluating statistical <br> reports | Evaluating statistical reports |

## Year 10A

## 1 Number and Algebra

### 1.1 Real numbers

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 5. Define rational and irrational numbers and perform operations with surds and fractional indices | Rational \& irrational numbers \& surds | Understanding rational \& irrational numbers |
|  |  | Introducing surds |
|  |  | Surd general rules |
|  |  | Simplification \& addition/subtraction of surds |
|  |  | Multiplying \& dividing surds |
|  |  | Expanding brackets with surds |
|  |  | Rationalising the denominator |
|  |  | Convert recurring decimals into rational numbers |
|  |  | Solving problems involving surds |
| 6. Use the definition of a logarithm to establish and apply the laws of logarithms and investigate logarithmic scales in measurement | Logarithms \& their laws | Introducing logarithms |
|  |  | Multiplication Log law |
|  |  | Division Log law 1 |
|  |  | Division Log law 2 |
|  |  | Log results |
|  |  | Log graphs \& relationship with exponentials |
|  |  | Solving equations with logarithms |

### 1.2 Patterns and algebra

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 7. Investigate the concept of a <br> polynomial and apply the factor <br> and remainder theorems to solve <br> problems | Polynomials | Introducing polynomials |

### 1.3 Linear and non-linear relationships

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 9. Describe, interpret and sketch <br> parabolas, hyperbolas, circles and | Functions \& their <br> transformations | Exploring parabolas |


| exponential functions and their transformations |  | Graphing parabolas |
| :---: | :---: | :---: |
|  |  | Parabolas \& their transformations |
|  |  | Graphing hyperbolas |
|  |  | Hyperbolas \& their transformations |
|  |  | Graphing circles |
|  |  | Circles \& their transformations |
|  |  | Exponential functions \& their transformations |
|  |  | General non-linear relationships |
| 10. Solve simple exponential equations | Solve exponential equations | Solving exponential equations |
| 11. Apply understanding of polynomials to sketch a range of curves and describe the features of these curves from their equation | Sketch polynomials | Sketching polynomials |
| 12. Factorise monic and non-monic quadratic expressions and solve a wide range of quadratic equations derived from a variety of contexts | Factorise \& solve quadratics | Factorising using difference of 2 squares |
|  |  | Factorising using grouping |
|  |  | Factorising using perfect squares |
|  |  | Factorising quadratic trinomials |
|  |  | Factorising complex fractions |
|  |  | Solving quadratic equations by factorisation |
|  |  | Solving quadratic equations: Completing the square |
|  |  | Solving quadratic equations with quadratic formula |
|  |  | Solving a variety of quadratic equations |
|  |  | The discriminant |
|  |  | Quadratic equations in context |

## 2 Measurement and Geometry

### 2.1 Using units of measurement

| Outcome | Quests | Content |
| :---: | :---: | :---: |
| 5. Solve problems involving surface area and volume of right pyramids, right cones, spheres and related composite solids | Surface area \& volume: composite solids | Finding surface area of pyramids \& cones |
|  |  | Finding surface area of spheres |
|  |  | Find dimensions of objects given the surface area |
|  |  | Surface area of composite solids |
|  |  | Volume of cones |
|  |  | Volume of spheres |
|  |  | Volume of composite solids |

### 2.2 Geometric reasoning

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 6. Prove and apply angle and chord <br> properties of circles | Properties of circles | Circle terminology |
| Circle properties: Tangents | Circle properties: Equal radii <br> Circle properties: Chord <br> properties |  |
|  |  |  |
|  | Circle properties: Angle <br> properties |  |
|  | Circle properties: Solve <br> problems using properties |  |

### 2.3 Pythagoras and trigonometry

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 7. Establish the sine, cosine and <br> area rules for any triangle and solve <br> related problems | Trigonometry: non <br> right-angled triangles | Sine rule |
|  |  | Cosine rule |
|  |  | Area rule |
|  | Solving problems in non-right- <br> angled triangles |  |
| 8. Use the unit circle to define <br> trigonometric functions as functions <br> of a real variable, and graph them | Trigonometry: <br> identities, ratios, angles | Using trigonometric identities |
|  | Investigating trigonometric <br> ratios |  |
|  |  | Angles of any magnitude |


| with and without the use of digital <br> technologies | Angle of inclination of a line <br> and its gradient |  |
| :--- | :--- | :--- |
| 9. Solve simple trigonometric <br> equations | Solve simple <br> trigonometric <br> equations | Solving simple trigonometric <br> equations |
| 10. Apply Pythagoras' theorem and <br> trigonometry to solving three- <br> dimensional problems in right- <br> angled triangles | Solve problems in three <br> dimensions | Solving problems in three <br> dimensions |

## 3 Statistics and Probability

### 3.1 Chance

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 1. Investigate reports of studies in <br> digital media and elsewhere for <br> information on their planning and <br> implementation | Critical analysis of data <br> in the media | Critical analysis of data in the <br> media |

### 3.2 Data representation and interpretation

| Outcome | Quests | Content |
| :--- | :--- | :--- |
| 2. Calculate and interpret the mean <br> and standard deviation of data and <br> use these to compare data sets. <br> Investigate the effect of individual <br> data values including outliers, on <br> the standard deviation | Mean \& standard <br> deviation | Using the mean \& standard <br> deviation of data sets |
| 3. Use digital technology to <br> investigate bivariate numerical data <br> sets. Where appropriate use a <br> straight line to describe the <br> relationship allowing for variation, <br> make predictions based on this <br> straight line and discuss limitations | Bivariate data \& lines <br> of best fit <br> standard deviation |  |

## Mathletics

## For more information about Mathletics, contact our friendly team.

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