Percentage Basics

Solutions





Copyright © 2009 3P Learning. All rights reserved.

First edition printed 2009 in Australia.

A catalogue record for this book is available from 3P Learning Ltd.

ISBN 978-1-921861-43-7

Ownership of content The materials in this resource, including without limitation all information, text, graphics, advertisements, names, logos and trade marks (Content) are protected by copyright, trade mark and other intellectual property laws unless expressly indicated otherwise.

You must not modify, copy, reproduce, republish or distribute this Content in any way except as expressly provided for in these General Conditions or with our express prior written consent.

Copyright Copyright in this resource is owned or licensed by us. Other than for the purposes of, and subject to the conditions prescribed under, the Copyright Act 1968 (Cth) and similar legislation which applies in your location, and except as expressly authorised by these General Conditions, you may not in any form or by any means: adapt, reproduce, store, distribute, print, display, perform, publish or create derivative works from any part of this resource; or commercialise any information, products or services obtained from any part of this resource.

Where copyright legislation in a location includes a remunerated scheme to permit educational institutions to copy or print any part of the resource, we will claim for remuneration under that scheme where worksheets are printed or photocopied by teachers for use by students, and where teachers direct students to print or photocopy worksheets for use by students at school. A worksheet is a page of learning, designed for a student to write on using an ink pen or pencil. This may lead to an increase in the fees for educational institutions to participate in the relevant scheme.

Published 3P Learning Ltd

For more copies of this book, contact us at: www.3plearning.com/contact/

Designed 3P Learning Ltd

Although every precaution has been taken in the preparation of this book, the publisher and authors assume no responsibility for errors or omissions. Neither is any liability assumed for damages resulting from the use of this information contained herein.

Page 3 questions

Proper fractions to percentages

1 a
$$\frac{9}{100} = 9\%$$

b
$$\frac{40}{100} = 40\%$$

$$\frac{75}{100} = 75\%$$

b
$$\frac{40}{100} = 40\%$$
 c $\frac{75}{100} = 75\%$ **d** $\frac{100}{100} = 100\%$

2 a
$$7\% = \frac{7}{100}$$

b
$$13\% = \frac{13}{100}$$

c
$$29\% = \frac{29}{100}$$

$$50\% = \frac{50}{100} = \frac{1}{2}$$
 Simplest Form

e
$$20\% = \frac{20}{100} = \frac{1}{5}$$
Simples

$$25\% = \frac{25}{100} = \frac{1}{4}$$
Simplest Form

$$75\% = \frac{75}{100} = \frac{3}{4}$$
Simplest Form

h
$$14\% = \frac{14}{100} = \frac{7}{50}$$
Simplest Form

1 55% =
$$\frac{55}{100} = \frac{11}{20}$$
Simples

$$78\% = \frac{78}{100} = \frac{39}{50}$$
Simplest Form

$$45\% = \frac{45}{100} = \frac{9}{20}$$
Simplest Form

$$68\% = \frac{68}{100} = \frac{17}{25}$$
Simplest Form

3 a
$$\frac{6}{200} = \frac{6 \div 2}{200 \div 2}$$

= $\frac{3}{100}$
= 3%

$$\frac{80}{400} = \frac{80 \div 4}{400 \div 4}$$

$$= \frac{20}{100}$$

$$= 20\%$$

$$\frac{150}{500} = \frac{150 \div 5}{500 \div 5}$$
$$= \frac{30}{100}$$
$$= 30\%$$

Page 4 questions

Proper fractions to percentages

3 d
$$\frac{7}{10} = \frac{7 \times 10}{10 \times 10}$$

= $\frac{70}{100}$
= 70%

$$\frac{5}{50} = \frac{5 \times 2}{50 \times 2}$$

$$= \frac{10}{100}$$

$$= 10\%$$

$$\frac{10}{25} = \frac{10 \times 4}{25 \times 4} \\
= \frac{40}{100} \\
= 40\%$$

4 a
$$\frac{1}{2} = \frac{1 \times 50}{2 \times 50}$$

= $\frac{50}{100}$
= 50%

b
$$\frac{3}{25} = \frac{3 \times 4}{25 \times 4}$$

$$= \frac{12}{100}$$

$$= 12\%$$

$$\begin{array}{c} \bullet \quad \frac{10}{10} = \frac{10 \times 10}{10 \times 10} \\ = \frac{100}{100} \\ = 100\% \end{array}$$

Page 4 questions

Proper fractions to percentages

4 d
$$\frac{3}{4} = \frac{3 \times 25}{4 \times 25}$$

$$=\frac{75}{100}$$

$$=\frac{60}{100}$$

$$=\frac{9}{100}$$

$$=\frac{99}{100}$$

h
$$\frac{50}{2500} = \frac{50 \div 25}{2500 \div 25}$$
 i $\frac{355}{500} = \frac{355 \div 5}{500 \div 5}$

$$=\frac{2}{100}$$

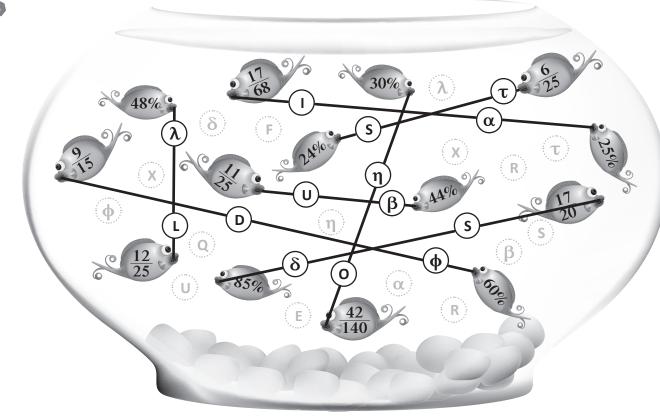
$$=\frac{71}{100}$$

$$= 71\%$$

Page 5 questions

Proper fractions to percentages

5





Page 7 questions

Decimals and percentages

 \blacksquare The percentage value is **divided by** 100, so the **decimal point** is **moved** 2 **places** to the left.

2 a
$$35 \div 100 = 0.35$$

= 0.35

b
$$75 \div 100 = 0.75$$
.

$$\begin{array}{c} \mathbf{C} \quad 32 \div 100 = 0 \overset{\checkmark}{\bullet} 32. \\ = 0.32 \end{array}$$

$$4 \div 100 = 0 \cdot 0 4.$$

$$= 0.04$$

$$\begin{array}{ccc}
\bullet & 1 \div 100 = 0 \cdot 0 1. \\
& = 0.01
\end{array}$$

The decimal is **multiplied by** 100, so the **decimal point** is **moved** 2 **places** to the right.

4 a
$$0.55 \times 100 = 0.55$$
.

b
$$0.23 \times 100 = 0.23$$
.

$$0.7 \times 100 = 0.70$$

$$= 70\%$$

d
$$0.8 \times 100 = 0.80$$

= 80%

$$0.01 \times 100 = 0.01.$$

$$= 1\%$$

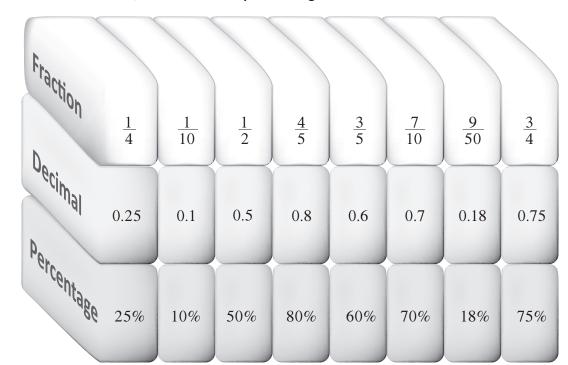
$$0.04 \times 100 = 0.04^{\circ}$$

$$= 4\%$$

Page 8 questions

Combo time: Decimals, fractions and percentages





Page 9 questions

Combo time: Decimals, fractions and percentages

2 **a** •
$$40 \div 100 = 0$$
 • 40.

$$= 0.4$$

•
$$\frac{40}{100} = \frac{2}{5}$$

b •
$$90 \div 100 = 0.9$$

= 0.9

 $\frac{90}{100} = \frac{9}{10}$

•
$$0.42 \times 100 = 0.42$$
• = 42%

$$\frac{42}{100} = \frac{21}{50}$$

d •
$$0.15 \times 100 = 0.15$$
.

$$\cdot \frac{15}{100} = \frac{3}{20}$$

$$\bullet \quad \frac{90 \div 2}{200 \div 2} = \frac{45}{100}$$

$$= 0.45$$
 Decimal

$$\bullet \frac{7 \div 2}{50 \div 2} = \frac{14}{100}$$

$$= 0.14$$
 Decimal

$$\bullet \quad \frac{1}{20 \times 5} = \frac{1}{100} = 0$$

b •
$$\frac{1 \times 5}{20 \times 5} = \frac{5}{100} = 0.05$$
 c • $36 \div 100 = 0.36$

•
$$\frac{8}{100} = \frac{2}{25}$$

•
$$\frac{5}{100} = 5\%$$

•
$$\frac{36}{100} = \frac{9}{25}$$

d •
$$\frac{6 \times 4}{25 \times 4} = \frac{24}{100} = 0.24$$
 e • $\frac{84 \div 3}{300 \div 3} = \frac{28}{100}$

 $\frac{24}{100} = 24\%$

$$\bullet \quad \cdot \frac{84 \div 3}{300 \div 3} = \frac{28}{100}$$

$$= 0.28$$

$$\frac{28}{100} = 28\%$$

$$\bullet \quad \frac{60 \div 15}{1500 \div 15} = \frac{4}{100} = \frac{1}{25}$$

$$= 0.04$$

•
$$\frac{4}{100}$$
 = 4%

Page 11 questions

Fractional and decimal percentages

1 a
$$\frac{2}{400} = \frac{0.5}{100} = 0.5\% = \frac{1}{2}\%$$
 b $\frac{3}{400} = \frac{0.75}{100} = 0.75\% = \frac{3}{4}\%$

Decimal Proper

Decimal

c
$$\frac{4}{500} = \frac{0.8}{100} = 0.8\% = \frac{4}{5}\%$$
 d $\frac{3}{750} = \frac{0.4}{100} = 0.4\% = \frac{2}{5}\%$

$$\frac{3}{750} = \frac{0.4}{100} = 0.4\% = \frac{2}{5}\%$$

2 a
$$\frac{15}{200} = \frac{7.5}{100} = 7.5\% = 7\frac{1}{2}\%$$
 b $\frac{10}{400} = \frac{2.5}{100} = 2.5\% = 2\frac{1}{2}\%$

Mixed number Decimal

b
$$\frac{10}{400} = \frac{2.5}{100} = 2.5\% = 2\frac{1}{2}\%$$

Decimal Mixed number

©
$$\frac{13}{500} = \frac{2.6}{100} = 2.6\% = 2\frac{3}{5}\%$$
 © $\frac{30}{800} = \frac{3.75}{100} = 3.75\% = 3\frac{3}{4}\%$

Decimal Mixed number

d
$$\frac{30}{800} = \frac{3.75}{100} = 3.75\% = 3\frac{3}{4}\%$$

Decimal Mixed number

Decimal Mixed number

Decimal Mixed number

g
$$\frac{47}{500} = \frac{9.4}{100} = 9.4\% = 9\frac{2}{5}\%$$
 h $\frac{75}{400} = \frac{18.75}{100} = 18.75\% = 18\frac{3}{4}\%$

Decimal Mixed number

Page 12 questions

Fractional and decimal percentages

a 0.105

b 0.3705

0.0245

d 0.0604

e 0.0075

0.00015

a 2.5%

b 6.25%

© 11.85%

e 45.05%

e 7.05%

0.96%





Page 12 questions

Fractional and decimal percentages

Decimal Mixed number

$$= 25\frac{1}{2}\% \qquad \qquad \textbf{0} \quad 0.085 \quad = \quad 8.5\% \qquad = \quad 8\frac{1}{2}\%$$

Decimal Mixed number

c
$$0.1025 = 10.25\% = 10\frac{1}{4}\%$$
 d $50.75 = 50.75\% = 50\frac{3}{4}\%$

Decimal Mixed number Decimal Mixed number

(e)
$$0.045 = 4.6\% = 4\frac{3}{5}\%$$
 (f) $0.084 = 8.4\% = 8\frac{2}{5}\%$ Decimal Mixed number



Page 14 questions

Percentage of an amount

1 a 25% of
$$20 = \frac{25}{100} \times 20$$

= 5

b 30% of
$$30 = \frac{30}{100} \times 30$$

= 9

c
$$40\%$$
 of $65 = 40 \div 100 \times 65$
= 0.4×65
= 26

d
$$45\%$$
 of $40 = 45 \div 100 \times 40$
= 0.45×40
= 18

b
$$\frac{50}{100} \times 18 = \frac{900}{100}$$

= 9

$$\frac{25}{100} \times 16 = \frac{400}{100}$$

$$= 4$$

$$\frac{75}{100} \times 28 = \frac{2100}{100} = 21$$

$$\frac{60}{100} \times 20 = \frac{1200}{100}$$
$$= 12$$

$$\frac{40}{100} \times 24 = \frac{960}{100}$$
$$= 9.6$$

$$\begin{array}{c} \mathbf{h} \quad \frac{20}{100} \times 39 = \frac{780}{100} \\ = 7.8 \end{array}$$

Page 15 questions

Percentage of an amount

$$(20 \div 100) \times 40 = 8$$

b
$$(30 \div 100) \times 20 = 6$$

$$(50 \div 100) \times 32 = 16$$

d
$$(35 \div 100) \times 80 = 28$$

$$(25 \div 100) \times 44 = 11$$

$$(75 \div 100) \times 18 = 13.5$$

$$(21 \div 100) \times 30 = 6.3$$

h
$$(19 \div 100) \times 25 = 4.75$$

Page 15 questions

Percentage of an amount

4 a
$$(40 \div 100) \times 45 = 18$$
 or $\frac{40}{100} \times 45 = \frac{1800}{100} = 18$

∴ 18 of the people were dressed as angels.

b
$$(15 \div 100) \times 200 = 30$$
 or $\frac{15}{100} \times 200 = \frac{3000}{100} = 30$

... Qian's music collection fills 30 GB of storage space.

Page 16 questions

Percentage of an amount

5 a
$$18\%$$
 = the word 'love', $\therefore 100\% - 18\% = 82\%$ of the words are not the word 'love'.

$$(82 \div 100) \times 150 = 123$$
 or $\frac{82}{100} \times 150 = \frac{12300}{100} = 123$

∴ 123 of the 150 words in Justin's poem are **not** the word 'love'

b
$$58\% = \text{prefer bananas}$$
, $\therefore 100\% - 58\% = 42\%$ prefer apples.

$$(42 \div 100) \times 800 = 336$$
 or $\frac{42}{100} \times 800 = \frac{33600}{100} = 336$

 \therefore 336 of the 800 fruit eating animals at the zoo preferred the taste of apples.

6 a
$$35\% + 14\% + 6\% = 55\%$$
, $100\% - 55\% = 45\%$ of the mixture is milk

$$(45 \div 100) \times 430 = 193.5$$
 or $\frac{45}{100} \times 430 = \frac{19350}{100} = 193.5$

:. there is 193.5 mL in the pancake mixture.

b 20% of
$$245 = (20 \div 100) \times 245$$

$$= 49 \, g$$

 $\therefore (245 - 49) = 196$ g left on the heaviest side

 \therefore total amount of weights on the scales = $2 \times 196 = 392$ g





Page 18 questions

Percentages greater than 100%

1 a
$$\frac{25}{20} = \frac{25 \times 5}{20 \times 5} = \frac{125}{100} = 125\%$$
 b $\frac{320}{200} = \frac{320 \div 2}{200 \div 2} = \frac{160}{100} = 160\%$

Equivalent Percentage fraction

b
$$\frac{320}{200} = \frac{320 \div 2}{200 \div 2} = \frac{160}{100} = 160\%$$

Equivalent Percentage fraction

$$\odot \frac{30}{25} = \frac{30 \times 4}{25 \times 4} = \frac{120}{100} = 120\%$$

c
$$\frac{30}{25} = \frac{30 \times 4}{25 \times 4} = \frac{120}{100} = 120\%$$
 d $\frac{720}{300} = \frac{720 \div 3}{300 \div 3} = \frac{240}{100} = 240\%$

2 a
$$1\frac{1}{2} = \frac{3}{2} = \frac{150}{100} = 150\%$$

Improper Fraction Percentage fraction

b
$$2\frac{1}{4} = \frac{9}{4} = \frac{225}{100} = 225\%$$

Improper Fraction Percentage fraction

$$1\frac{4}{5} = \frac{9}{5} = \frac{180}{100} = 180\%$$

d
$$3\frac{13}{10} = \frac{43}{10} = \frac{430}{100} = 430\%$$

e
$$2\frac{12}{25} = \frac{62}{25} = \frac{248}{100} = 248\%$$
 f $1\frac{17}{20} = \frac{37}{20} = \frac{185}{100} = 185\%$

$$1\frac{17}{20} = \frac{37}{20} = \frac{185}{100} = 185\%$$

3 a
$$120\% = \frac{120}{100} = 1\frac{20}{100} = 1\frac{1}{5}$$
 b $270\% = \frac{270}{100} = 2\frac{70}{100} = 2\frac{7}{10}$

Improper Mixed Simplified fraction number Simplified fraction number

b
$$270\% = \frac{270}{100} = 2\frac{70}{100} = 2\frac{7}{10}$$

Improper Mixed Simplified number

©
$$110\% = \frac{110}{100} = 1\frac{10}{100} = 1\frac{1}{10}$$
 © $475\% = \frac{475}{100} = 4\frac{75}{100} = 4\frac{3}{4}$

d
$$475\% = \frac{475}{100} = 4\frac{75}{100} = 4\frac{3}{4}$$

e
$$355\% = \frac{355}{100} = 3\frac{55}{100} = 3\frac{11}{20}$$
 f $192\% = \frac{192}{100} = 1\frac{92}{100} = 1\frac{23}{25}$

f
$$192\% = \frac{192}{100} = 1\frac{92}{100} = 1\frac{23}{25}$$

Page 19 questions

Percentages greater than 100%

$$213\% = 213 \div 100 = 2.13$$

$$490\% = 490 \div 100 = 4.90$$

$$300\% = 300 \div 100 = 3.00$$

b
$$2.35 = 2.35 \times 100\% = 235\%$$

d
$$1.68 = 1.68 \times 100\% = 168\%$$

h
$$4.5 = 4.5 \times 100\% = 450\%$$

a
$$212.5 \div 100 = 2.125$$

$$165\frac{1}{2} = 165.5$$

$$\therefore 165.5 \div 100 = 1.655$$

$$2.125 \times 100 = 212.5\%$$

$$\therefore 212.5\% = 212\frac{1}{2}\%$$

$$3.004 \times 100 = 300.4\%$$

$$\therefore 300.4\% = 300\frac{2}{5}\%$$

b
$$105.75 \div 100 = 1.0575$$

d
$$286\frac{1}{4} = 286.25$$

$$\therefore 286.25 \div 100 = 2.8625$$

h
$$1.902 \times 100 = 190.2$$

$$\therefore 190.2\% = 190\frac{1}{5}\%$$

$$\bigcirc$$
 2.0075 × 100 = 200.75%

$$\therefore 200.75\% = 200\frac{3}{4}\%$$

Page 21 questions

Recurring decimal percentages

1 a
$$55.5\% = 55\frac{5}{9}\%$$

b
$$122.\dot{2}\% = 122\frac{2}{9}\%$$

6
$$64.\dot{4}\% = 64\frac{4}{9}\%$$

d
$$23.\dot{2}\dot{3}\% = 23\frac{23}{99}\%$$

e
$$8.\dot{0}\dot{8}\% = 8\frac{8}{99}\%$$

1
$$10.\dot{1}\dot{2}\% = 10\frac{12}{99}\% = 10\frac{4}{33}\%$$

10

Page 21 questions

Recurring decimal percentages

a
$$0.00\dot{2} \times 100 = 0.\dot{2}\%$$

$$=\frac{2}{9}\%$$

b
$$0.00\dot{7} \times 100 = 0.\dot{7}\%$$

$$=\frac{7}{9}\%$$

$$0.02\dot{5} \times 100 = 2.\dot{5}\%$$

$$=2\frac{5}{9}\%$$

d
$$0.06\dot{4} \times 100 = 6.\dot{4}\%$$

$$=6\frac{4}{9}\%$$

$$0.0\dot{8} \times 100 = 8.\dot{8}\%$$

$$=8\frac{8}{9}\%$$

f
$$0.\dot{1} \times 100 = 11.\dot{1}\%$$

$$=11\frac{1}{9}\%$$

g
$$0.\dot{3} \times 100 = 33.\dot{3}\%$$

$$=33\frac{1}{3}\%$$

h
$$0.9\dot{8} \times 100 = 98.\dot{8}\%$$

$$=98\frac{8}{9}\%$$

$$0.2\dot{6} \times 100 = 26.\dot{6}\%$$

$$=26\frac{2}{3}\%$$

3 a
$$2\frac{4}{9}\% = 2.4\%$$

$$\therefore 2.\dot{4} \div 100 = 0.02\dot{4}$$

$$4\frac{16}{18}\% = 4\frac{8}{9}\% = 4.8\%$$

$$\therefore 4.\dot{8} \div 100 = 0.04\dot{8}$$

$$1\frac{2}{3}\% = 1\frac{6}{9}\% = 1.6\%$$

$$1.6 \div 100 = 0.016$$

Page 23 questions

One amount as a percentage of another

1 a 5 out of
$$20 = \frac{5}{20}$$

= $\frac{25}{100}$
= 25%

$$= \frac{25}{100} = 25\%$$

$$= 25\%$$

$$= 40\%$$

d 450 out of
$$500 = \frac{450}{500}$$

= $\frac{90}{100}$
= 90%

b 10 out of $25 = \frac{10}{25}$

2 a 12 out of
$$32 = \frac{12}{32}$$

= $[(25 \div 32) \times 100]\%$
= 37.5%
= $37\frac{1}{2}\%$

b 21 out of
$$24 = \frac{21}{24}$$

= $[(21 \div 24) \times 100]\%$
= 87.5%
= $87\frac{1}{2}\%$

© 25 out of
$$30 = \frac{25}{30}$$

= $[(25 \div 30) \times 100]\%$
= 83.3%
= $83\frac{1}{3}\%$

d 10.1 out of
$$40 = [(10.1 \div 40) \times 100]\%$$

= 25.25%
= $25\frac{1}{4}\%$

3 a 4 out of
$$9 = \frac{4}{9}$$

= $[(4 \div 9) \times 100]\%$
= 44.4%
= 44.44 (to 2 d.p.)

13 out of
$$33 = \frac{13}{33}$$

= $[(13 \div 33) \times 100]\%$
= $39.\dot{3}\dot{9}\%$
= 39.39 (to 2 d.p.)

Page 23 questions

One amount as a percentage of another

3 **c** 8.9 out of $11 = [(8.9 \div 11) \times 100]\%$

$$= 80.\dot{9}\dot{0}\%$$

$$= 80.91\%$$
 (to 2 d.p.)

d 22.8 out of $34 = [(22.8 \div 34) \times 100]\%$

= 67.058 823 53%

= 67.06% (to 2 d.p.)

Page 24 questions

One amount as a percentage of another

- $= [(48 \div 50) \times 100]\%$
 - = 96%
 - ∴ Grace spelled 96% of the words correctly in the test.
- $= [(16 \div 25) \times 100]\%$
 - = 64%
 - ∴ 64% of Luke's passes were good.
- 6 Two of the covers have a striped pattern and there are eight different covers altogether.

$$= [(2 \div 8) \times 100]\%$$

- = 25%
- ∴ 25% of covers available have a striped pattern.
- Green is one of the seven different main dispersed light colours.

$$= [(1 \div 7) \times 100]\%$$

- = 14.285 714 29%
- = 14.29% (to 2 d.p.)

The colour green makes up 14.29% of the dispersed white light.

Page 25 questions

One amount as a percentage of another

8 =
$$[(0.82 \div 3.6) \times 100]\%$$

= 22.7%
= 22.8% (to 1 d.p.)

∴ 22.8% of the cordial is syrup flavour.

$$= [(14 \div 39) \times 100]\%$$

$$= 35.897 435 9...\%$$

$$= 35.9\% \text{ (to 1 d.p.)}$$

... One song contains 35.9% of all the different chords the band plays in one show.

$$= [(12.6 \div 16) \times 100]\%$$

$$= 78.75\%$$

$$= 78\frac{3}{4}\%$$

∴ Nicola has already used $78\frac{3}{4}\%$ of the memory stick storage space.

Of the fifteen hexagons, eight of them are shaded black.

$$= [(8 \div 15) \times 100]\%$$

$$= 53.3\%$$

$$= 53\frac{1}{3}\%$$

 $\therefore 53\frac{1}{3}\%$ of the hexagons are shaded black.

1 There are four pink wrapped chocolates, and eighteen wrapped chocolates altogether.

$$= [(4 \div 18) \times 100]\%$$

$$= 22.2\%$$

$$= 22\frac{2}{9}\%$$

 $\therefore 22\frac{2}{9}\%$ of the chocolates have pink foil.





Page 26 questions

One amount as a percentage of another

- $(22 \div 25) \times 100 \,]\% = 88\%$
 - ∴ 88% of the students had completed their homework.
- If 35 voted 'yes', then 67 35 = 32 voted 'no'.

$$= [(32 \div 67) \times 100]\%$$

$$=47.76119403$$

$$= 47.8\%$$
 (to 1 d.p.)

 \therefore 47.8% of the people at the meeting voted 'no'.

$$= [(4+3+5) \div (4+3+5+2) \times 100]\% = 88\%$$

$$= [[12 \div 14] \times 100]\% = 85.7\% \text{ (to 1 d.p.)}$$

 \therefore 85.7% of the movies were not romantic comedies.

$$(41500 - 19173) = 22327$$
$$[(22327 \div 41500) \times 100]\% = 53.8\%$$
$$= 53\frac{4}{5}\%$$

 $\therefore 53\frac{4}{5}\%$ of the supporters left the game disappointed.







16

