

Algebra Basics







Copyright © 2009 3P Learning. All rights reserved.

First edition printed 2009 in Australia.

A catalogue record for this book is available from 3P Learning Ltd.

ISBN 978-1-921861-24-6

Ownership of content The materials in this resource, including without limitation all information, text, graphics, advertisements, names, logos and trade marks (Content) are protected by copyright, trade mark and other intellectual property laws unless expressly indicated otherwise.

You must not modify, copy, reproduce, republish or distribute this Content in any way except as expressly provided for in these General Conditions or with our express prior written consent.

Copyright Copyright in this resource is owned or licensed by us. Other than for the purposes of, and subject to the conditions prescribed under, the Copyright Act 1968 (Cth) and similar legislation which applies in your location, and except as expressly authorised by these General Conditions, you may not in any form or by any means: adapt, reproduce, store, distribute, print, display, perform, publish or create derivative works from any part of this resource; or commercialise any information, products or services obtained from any part of this resource.

Where copyright legislation in a location includes a remunerated scheme to permit educational institutions to copy or print any part of the resource, we will claim for remuneration under that scheme where worksheets are printed or photocopied by teachers for use by students, and where teachers direct students to print or photocopy worksheets for use by students at school. A worksheet is a page of learning, designed for a student to write on using an ink pen or pencil. This may lead to an increase in the fees for educational institutions to participate in the relevant scheme.

Published 3P Learning Ltd

For more copies of this book, contact us at: www.3plearning.com/contact/

Designed 3P Learning Ltd

Although every precaution has been taken in the preparation of this book, the publisher and authors assume no responsibility for errors or omissions. Neither is any liability assumed for damages resulting from the use of this information contained herein.





• Triangles have been stacked to form an increasing number pattern below:



How many small triangles would be needed to make the 15th picture in this pattern?





8



1



Words and symbols

Algebra uses letters or symbols called variables. Each part in an algebraic expression is called a term.



Let's look at another similar expression.



Algebraic expressions with an equals sign '=' are called equations.



Here's another one.







Η	ow does it work?	Your Turn	Algebra Basics
A	Words and symbols		WORDS AND
1	Write down the variable in each of t	the following mathemati	cal statements://20
	a 12 + b	b 3 - m +	2 SYMBUL
	$\bullet 7 \times k + 3$	d $2a + 3a$	1
2	Circle each of the algebraic expressi	ions below in which the v	variable can be any value:
	$5 \times w = 30$	x -	$\div x = 1$ $32 - 2 \times d = 16$
	3 + x =	$12 \times g =$	
	$200 \div s = 25$		$3 \times x + 6 =$
3	Match up each of the algebraic exp	ressions with the correct	outcome using the given variable value:
	11 - x if $x = 4$ •	• 20	
	$4 \times m$ if $m = 5$ •	• 10	
	$27 \div a$ if $a = 3$ •	• 9	
	$1 + 3 \times z$ if $z = 3$ •	• 7	
4	Write down the value of the variabl	e that makes these equa	tions equal on both sides:
	a) $12 + c = 20$	b 14 - h =	= 2
	c =	<i>h</i> =	=
	$k \div 3 = 6$	d 12 × y =	= 72
	k =	<i>y</i> =	=



3



How does it work?

Multiplication

Instead of writing $5 \times m$ or $a \times b$, we simply write 5m or ab to mean the exact same thing!

Always put the number first.

Simplify $3 \times 2 \times n$

 $3 \times 2 \times n = 6 \times n$

= 6n

If multiplying by 1, do not write 1 in front of the variable.

Simplify $1 \times y$

 $1 \times y = y \pmod{1y}$

 1×2 is just 2. The same rule applies when multiplying a variable by 1

The 1 is hidden

Write multiplied variables in alphabetical order.

Simplify $2 \times p \times 5 \times r \times q$ $2 \times p \times 5 \times r \times q = 2 \times 5 \times p \times r \times q$ Re-order with numbers first $= 10 \times p \times r \times q$ Multiply the numbers first = 10pqrPut variables in alphabetical order

Use powers to simplify multiplications of the same variable.

Simplify $a \times a \times b$ $a \times a \times b = a^2 \times b$ $= a^2 b$ Just like 4×4 is 4^2 , $a \times a$ is a^2

Doing the opposite of these examples is called **expanding**. Write a^2b in expanded form

Simplified form



Expanded form

 $\therefore a^2 b = a \times a \times b$



Algebra Basics

Multiply the numbers together







Η	ow does it work?	Your Turn	Algebra Basics	
À	Multiplication		Multiplication	
1	Simplify: (psst: remember the ru	les!)	AT/20	
	a $2 \times 7 \times k$	b <i>u</i> × 1	C 5×r×p	
	d $n \times m \times m$	• $6 \times b \times 3 \times b$	• $4 \times j \times l \times 3 \times k$	
2	Expand each of these			
	a 4 <i>pq</i>	b $4a^2$	$\bigcirc 3m^2n$	

It's combo time! Calculate the value of these expressions using the variable in the square brackets.

a) $3x + 2$	[x = 4]	b 15 – 2 <i>b</i>	[b = 6]
-------------	---------	--------------------------	---------

c $3 \times 5g$ [g = 2] **d** $4m^2$ [m = 3]



5





How does it work?

Division

When dividing two algebraic terms it sometimes helps to write the division as a fraction first. $\mathbb Z$



Aways write fractions in simplest form.



Brackets are not necessary for simple divisions written in fraction form.





$$\therefore \frac{y}{4+x} = y \div (4+x)$$

brackets or (parentheses)



Algebra Basics

 $a \div b = \frac{a}{b}$









7



 $e x \times x \div (y + 2x)$ $f d \times f \times d \div (11 + f \times e)$

2 Expand these by re-writing with multiplication/division signs and grouping symbols:





8



CON

Phrases as algebraic expressions

To solve problems with algebra we use **variables** to turn the problem into an algebraic rule (or relationship).



Write a rule for: the difference between a number and 3 minus Let the number be n $\therefore n-3$

The order of the words in a sentence makes a difference to which operation is done first.

	Write a rule for: the difference between double a number and 3
	minus multiply by 2
	Let the number be <i>n</i>
	$\therefore 2n-3$
	a number doubled, minus 3
~	

Write a rule for: double the difference between a number and 3 multiply by 2 minus Let the number be n $\therefore 2(n-3)$ Brackets used because n-3 is calculated first \therefore double the difference between a number and 3

 Write a rule for: the quotient of 4 times a number and 3

 divide
 Let the number be n

 anumerator $\therefore \frac{4n}{3}$

 4n was first in the sentence, so it is the numerator





Use a variable







Phrases as algebraic expressions

- Write these phrases as algebraic expressions (let the number be 'n')
 - a The sum of a number and 7:

How does it work?



Your Turn

- **b** The difference between 9 and a number:
- **c** The sum of 6 times a number and 1:
- **d** The product (×) of a number and 4:
- The quotient (÷) of two more than a number and 3:
- **(f)** The difference between a number squared and 6:
- **g** The product of a number minus 5 and 2:
- **b** 8 less than twice a number:
- 10 added to a number halved: 0
- I A number multiplied by 5 more than itself:





How does it	work?	Your Turn	Algebra	Basics
Phras	es as algebraic	expressions		1
2 Circle whether	the algebraic expressi	on is correct or incorre	ect for each phrase.	
a A number n	nultiplied by 4 added to	o 7:	Cor	rect Incorrect
		4 <i>n</i> + 7		
b The differer	nce between a number	and 4:	Cor	rect Incorrect
		4 - n		
C The sum of	6 and the product of 3	and a number:	Cor	rect Incorrect
		3n + 6		
d The quotier	nt of 4 plus a number a	nd 9:	Cor	rect Incorrect
		$4 \div (n+9)$		
e A number d	livided by 5 and added	to the number:	Cor	rect Incorrect
		$\frac{n}{5}$ + 5		
f A number ti	imes the difference be	tween the number and	l one: Cor	rect Incorrect
		n(n-1)		
g The sum of	a number, and three m	ninus the number halve	ed: Cor	rect Incorrect
		$n + \frac{3-n}{2}$		
h The product	t of 6 more than twice	a number and 4:	Cor	rect Incorrect
		4(2n+6)		
The product	t of a number squared	and 3:	Cor	rect Incorrect
		$(3n)^2$		
The quotier	nt of 5 less than a numl	per and the number:	Cor	rect Incorrect
		n-5		



n

Mathletics

How does it work?

Only 'like terms' can be added or subtracted.

Simplify $2a + a$
2a + a \uparrow \uparrow Variable parts are the same (like terms)
$\therefore 2a + a = 3a$

Simplify 8x - 3x

```
8x - 3x
```

```
\therefore 8x - 3x = 5x
```

Simplify 3d + 4d + 6c 3d + 4d + 6c \uparrow like terms 3d + 4d + 6c = 7d + 6c This cannot be simplified any further

Why don't we add or subtract unlike terms? Good Question!

Let's look at a problem the last example could represent.

At a picnic for pets, each dog gets 7 treats and each cat gets 6 treats. Number of treats needed is: (7 treats × number of dogs) + (6 treats × number of cats)

$$= (7 \times d) + (6 \times c)$$

the number of dogs the number of cats



d and c represent two different animals so it does not make sense to add them together.

Simplified: = 7d + 6c

Therefore 7d + 6c is the **simplest expression** for this problem.



H	ow does it work?	Your Turn	Algebra Basics
1	Addition and subtract Simplify:	b 3 <i>u</i> + 5 <i>u</i>	Addition and HADDITAL SUbtraction
	c 14 <i>r</i> – 9 <i>r</i>	d 4g – 7g	
	e 6 <i>m</i> − 8 <i>m</i>	($-11x + 2x$	
	g $7y + 2y + 4y$	b 30 <i>p</i> – 15 <i>p</i> –	- 10 <i>p</i>
2	Simplify: (psst: look for the like term	s!)	
	a) $13m + 9n + 12m$	b 14 <i>a</i> + <i>b</i> + 1	0 <i>b</i>
	c $16x + 9y + 15y$	₫ 9 <i>d</i> − 5 <i>c</i> − 3	d
	c $7e + 11e + 2a$	f 13g - 15g -	- 4h

Algebra Basics

Mathletics © 3P Learning Ltd



How does it work?

Grouping like terms

Terms can have the same variable letter but still not be 'like terms'.

Simplify $7a + 3a^2 + a + 2a^2$	
• <i>a</i> is different to a^2 so they are not like terms.	
$\therefore 7a + 3a^{2} + a + 2a^{2} = 7a + a + 3a^{2} + 2a^{2}$ $= 8a + 5a^{2}$	Grouping the like terms

Each term of an expression includes the sign in front of it.

Simplify
$$9j - 11k + 5j + 8k$$

no sign in front mean +
 $9j - 11k + 5j + 8k = 9j - 11k + 5j + 8k$
 $= 9j + 5j - 11k + 8k$ Grouping the like terms
 $= 14j - 3k$ Simplify

It's helpful to circle the like terms with similar shapes, including the sign in front.

Here are two more examples that combine two simplifying concepts.

Simplify and write in fraction form:
$$(5a + 4b - 2a) \div 3b$$

 $((5a) + 4b - 2a) \div 3b = (3a + 4b) \div 3b$ Simplify the bracket
 $= \frac{3a + 4b}{3b}$ Write division as a fraction

Simplify each bracket and write in fraction form: $(x - 2x^2 + 8x) \div (13x^2 + 8x^2 - 5x)$

$$(x - 2x^2 + 8x) \div (13x^2 + 8x^2 - 5x) = (9x - 2x^2) \div (21x^2 - 5x)$$
Simplify the bracket
$$= \frac{9x - 2x^2}{21x^2 - 5x}$$
Write division as a fraction



-3a



Algebra Basics

Same character but not alike

it work?____

14

TODIC



Combo time!

2 Simplify and write in fraction form:

a $11y \div (2y + 2x - y)$ **b** $(7p^2 - 5p - 8p^2) \div 12$

3 Simplify each bracket and write in fraction form:

a $(2x - 3y + 2x) \div (4x + 3x - 2y)$ **b** $(2 \times 4a + 3 \times 2b) \div (3 \times a \times a + 2a^2)$







Square steps = multiply Circle steps = divide Trapezium steps = add Pentagon steps = subtract Remember, like terms only!

Starting with a value of $4x^2$, travel along the lines from step to step until you get to the outer edge. Each step affects your value.

If you have exactly 2x left when you reach one of the shapes at the outer edge, then you have escaped! Good luck.

How many paths can you find to get away from Algebra Island?

How many steps is the longest path you can find?





How does it work?

Algebra Basics

Bringing all the previous concepts together



These examples combine the different simplifying concepts together.



The fancy name given to doing this sort of thing in Mathematics is substitution.

Calculate the value of $5x + 2y$ when $x = 2$ and $y = 6$
$5x + 2y = 5 \times 2 + 2 \times 6$ Substitute the value of the variables. x = 2 $y = 6$
= 10 + 12
= 22

Where possible, simplify the expression first before substituting in the variable values.

Evaluate 4m + 3n - 2m + 5n when m = 6 and n = -3• Simplify: 4m + 3n - 2m + 5n Identify the like terms and their sign = 4m - 2m + 3n + 5n Group the like terms = 2m + 8n Simplify • Evaluate: $2m + 8n = 2 \times 6 + 8 \times -3$ Substitute in the variable values "find the value of" m = 6 n = -3 = 12 - 24= -12





17

How does it work?

The same variable value can be substituted into unlike terms.

Evaluate
$$3p^2 + 8p - p^2 - 3p$$
 when $p = 2$
• Simplify:
 $(3p^2) + 8p - p^2 - 3p$
 $= (3p^2 - p^2) + 8p - 3p$
 $= (3p^2 - p^2) + 8p - 3p$
 $= 2p^2 + 5p$
• Evaluate:
 $2p^2 + 5p = 2 \times 2^2 + 5 \times 2$
 $p = 2$
 $= 2 \times 4 + 5 \times 2$
 $= 8 + 10$
 $= 18$
Udentify the like terms and their sign
Group the like terms
Substitute in the variable value

Checkout these two extra examples...

Evaluate $\frac{2x+y}{3x}$ when $x = 1$	3 and $y = 12$	
Remember: <u>numerator</u> denominator	$\frac{2x+y}{3x} = \frac{2 \times 3 + 12}{3 \times 3}$	Substitute in the variable values
32	$= \frac{6+12}{9} = \frac{18}{9} (18 \div 9) = 2$	Simplify the numerator and denominator Simplify the fraction
Evaluate 2m ² n when m = 2	and n 7	

Evaluate
$$2m^2n$$
 when $m = 2$ and $n = 7$
• Evaluate:
 $2m^2n = 2 \times m^2 \times n$ Expanded form
 $2 \times m^2 \times n = 2 \times 2^2 \times 7$ Substitute in the variable values
 $m = 2$ $n = 7$
 $m = 2 \times 4 \times 7$ Multiply terms together
 $= 56$







2 Calculate the value of these expressions when a = -2 and b = 5

a a + 2b **b** 3b - 6a

c
$$\frac{24}{a+b}$$
 d $\frac{a^2b}{4}$

3 Evaluate these expressions when c = 6, d = 9

a c + d + 2c + 3d **b** 2c + d + 3c - d

c
$$\frac{2d-c}{d-c}$$
 d $(c+d) \times (2c-d)$





Algebra Basics



Bringing all the previous concepts together

Give these three variable questions a go!

4 Evaluate these expressions when x = 6, y = 3 and z = -8

a)
$$2x + y + z$$
 b) $3z + xy$



$$d \frac{4y}{x+z}$$

Earn an Awesome passport stamp with these questions:

5 Evaluate
$$\frac{a(a+2b)^2}{(b-a)^2}$$
 when $a = 2$, $b = -4$



, a, b & c

6 Evaluate
$$\left[\frac{(x-y)^2}{(y-x)^2}\right]^2$$
 when $x = -1$, $y = -5$





Tables of values

These are used to show how one variable changes when another variable in a given **rule** is changed.

Complete the table of values using the rule: $b = a + 3$								
	а	0	1	2	3	4	5	
	b							
• Substitu	Substitute each value of <i>a</i> into the rule to find <i>b</i>							
	а	0	1	2	3	4	5	
	b	3	4	5	6	7	8	
	a = 0							
		$\therefore b = 0 + 3$	$\therefore b = 1 + 3$	$\therefore b = 2 + 3$	$\therefore b = 3 + 3$	$\therefore b = 4 + 3$	$\therefore b = 5 + 3$	
		$\left = 3 \right $	= 4	= 5	= 6	[= 7]	= 8	

Complete the table of values using the rule: $y = \frac{x}{3}$									
	x	3	6	9	12	15	18		
	у	1	2	3	4	5	6		
		$\begin{array}{c} x = 3 \\ \therefore y = 3 \div 3 \\ = 1 \end{array}$	x = 6 $\therefore y = 6 \div 3$ y = 2	x = 9 $\therefore y = 9 \div 3$ y = 3	x = 12 $\therefore y = 12 \div 3$ y = 4	x = 15 $\therefore y = 15 \div 3$ y = 5	x = 18 $\therefore y = 18 \div 3$ y = 6		

Cor	Complete the table of values using the rule: $m = 3n - 1$								
	п	0	1	2	3	4	5		
	т	-1	2	5	8	11	14		
		n = 0	n = 1	n = 2	n = 3	n = 4	n = 5		
		$\therefore m = 3 \times 0 - 1$ $= -1$	$\therefore m = 3 \times 1 - 1$ $= 2$	$\therefore m = 3 \times 2 - 1$ $= 5$	$\therefore m = 3 \times 3 - 1$ $= 8$	$\therefore m = 3 \times 4 - 1$ $= 11$	$\therefore m = 3 \times 5 - 1$ $= 14$		





Your Turn

b c = 2d

d

С

y

0

1

TĄ



Table of values

① Complete each table of values using the given rule.

a u = v + 2



c g = 4h - 3

h	1	2	3	4	5
g					

d	<i>y</i> =	$\frac{x}{2} + 1$				
	x	2	4	6	8	10

2

3

4

2

Draw lines to match each table of values with the correct matching rule.

a	0	2	4	6	8		$b - 2a \pm 3$
b	2	3	4	5	6	•	• $b = 2a + 5$
a	1	2	3	4	5		a + 4
b	1	6	11	16	21	•	• $b = \frac{a+4}{2}$
	0		•				
a	0	1	2	3	4	•	h - 3a
b	0	3	6	9	12	•	• <i>b</i> = 3 <i>a</i>
a	0	1	2	3	4		L 5 a 1
b	3	5	7	9	11	•	• $b = 5a - 4$



B Have a go at figuring out the rule used for each table of values below and fill in the gaps.

a Rule:

x	0	1	2	3	4
у	5	6			9

C Rule:

p	0	1	2	3	4
q	-3		-1		1



22





d Rule:

С		1		5	6
d	-5	-1	3		19



Number patterns

There are a lot of patterns in the world and it is a useful skill to be able to work them out.



The number pattern formed can be displayed using a table of values:





23



Number patterns

For each of these pattern diagrams:

- (i) Describe the number pattern formed by the shapes
- (ii) Write a number pattern for the total number of shapes used to make the first five diagrams



SERIES

TOPIC



For each of these pattern diagrams: 2

- (i) Complete a table of values for the first 4 diagrams
- (ii) Write down how many shapes are needed for the 7th diagram



(ii) Number of hearts needed for the 7th diagram = ____



(ii) Number of hexagons needed for the 7th diagram = _____



(1)	Diagram number	1	2	3	4
	Number of matchsticks				

(ii) Number of matchsticks needed for the 7th diagram = _____





Algebra Basics

Mathletics © 3P Learning Ltd

26

'find the algebra rule for the pattern'. Find the algebraic rule for the matchstick pattern below:

Modelling number patterns

Where does it work?

Modelling a number pattern is the fancy way Mathematicians say:





m=2t + 1

Algebra Basics

Where does it work?	Your Turn	Algebra Basics
Modelling number	patterns	PATTERNS * MODELLI
Write down the general rule for each o	f the following matchstic	k number patterns:
	,	THE CALL & SINTETTING
Let <i>s</i> be the number of squares an	d <i>m</i> the number of match	nsticks
Number of squares (s)		General rule:
Number of matchsticks (m)		$m = $ $\times s + $
•		<u> </u>
Let t be the number of triangles an	nd m the number of matc	hsticks
Number of triangles (t)		General rule:
Number of matchsticks (m)		$m = _ t + _$
3 () , ()	,	,
Let <i>r</i> be the number of grey rings	and <i>c</i> the number of circle	es drawn
Number of grey rings (r)	1	General rule:
Number of circles drawn (c)	2	c = $r +$
	,	,
Let p be the number of pentagonal	I shapes and t the numbe	er of triangles used
Number of pentagonal shapes (p)		General rule:
Number of triangles (t)		t = p
		¹

SERIES TOPIC



Mathletics

Where does it work?

More number pattern modelling

The diagram number (n^{th} diagram) and the number of shapes in each diagram is used for these questions.



This method also works for matchstick patterns.







Your Turn



1

More number pattern modelling

Write down the general rule for each of the following matchstick number patterns:





Let *n* be the diagram number and *m* the number of matchsticks







Let *n* be the diagram number and *m* the number of matchsticks

Diagram number (n)		
Number of matchsticks (m)		

Ger	eral	rule:	
		······	Ĩ

m =		n	+	
-----	--	---	---	--





Let *n* be the diagram number and *m* the number of matchsticks

Diagram number (n)		0
Number of matchsticks (m)		ľ

General rule:



SERIES

TOPIC

d 1 st



Let *n* be the diagram number and *m* the number of matchsticks

Diagram number (n)		General rule:	
Number of matchsticks (m)		$ \qquad \qquad m = \left[\begin{array}{c} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$	





More number pattern modelling

Write down the general rule for each of the following number patterns:



Let s be the number of snow flakes and n the n^{th} diagram

Diagram number (n)		
Number of snow flakes (s)		





Where does it work?







Let t be the number of tyres and n the n^{th} diagram

Diagram number (<i>n</i>)		
Number of tyres (<i>t</i>)		





Let d be the number of dots and n the nth diagram

Diagram number (n)		
Number of dots (<i>d</i>)		











Let t be the number of triangles formed and n the n^{th} diagram

Diagram number (n)		General	rule:	ç	<u>.</u>	£
Number of triangles (<i>t</i>)		=	×			

There are actually two number patterns here, the other involves the number of matchsticks used. See if you can work it out!



Using the general rule

Substitution into the general rule is used to answer questions about the n^{th} diagram in a pattern.



Find the general rule for the matchstick number pattern:



Let *m* be the number of matchsticks and *n* the n^{th} diagram



How many matchsticks are there in the 8th diagram?

 $\therefore m = 5 \times 8 - 2$ Substitute n = 8 into the general rule = 38 matchsticks





Your Turn

GEN

THE

RULE



Using the general rule

Every time Niamh kicked a goal (g) the team score (s) increased by 2.
 The general rule for this is given by:

$$s = 2g$$

How many points did Niamh score after kicking g = 8 goals?

b If the total number of chickens (c) that crossed the road after each minute (m) is given by the general rule: c = 5m - 3

How many chickens had crossed the road when m = 7 minutes?

C The total number of shirts (s) tried on by customers (c) in a store is represented by the general rule:

$$s = 2c + 1$$

How many shirts had been tried on when there were c = 12 customers?

In total number of vegetarian meals (v) ordered (on average) in a restaurant by diners (d) is given by the general rule:

$$v = \frac{d}{3}$$

How many vegetarian meals were ordered on a night with d = 36 diners?









Using the general rule

2 The stacked tyres below form a number pattern. Find the general rule and then calculate how many tyres are in the 12th stack.



New leaves are appearing on a tree each day forming a number pattern. Find the general rule and calculate how many leaves there are on the 10th day.



, Day 2



Let l be the number of leaves and n the n^{th} day.

п		
l		

General rule:

Leaves on the 10^{th} day:

The basketballs represent the number of good shots during each training session. The good shots are increasing by the same amount each time. How many good shots are made during the 8th session?









Let s be the number of good shots and n the nth training session.

п		
S		

General rule:

Good shots in the 8th session:







Using the general rule

A tiler is laying out some octagonal tiles in the following number pattern:







 $1^{\,\rm st}\,{\rm diagram}$

How many tiles will be laid in the 12^{th} diagram? let *t* be the number of tiles laid and *n* the *n*th diagram.

п		
t		

General rule:

Tiles laid in the $12^{\mbox{\tiny th}}$ diagram:



6 Triangles have been stacked to form an increasing number pattern:







Find the general rule and calculate the number of triangles needed for the 15^{th} shape. Let *t* be the number of trangles and *n* the n^{th} shape.

п		
t		

General rule:

Triangles in the 15^{th} shape:







Table of values

These show how one variable changes when another variable in a given rule is changed



Modelling number patterns

This is a fancy way Mathematicians say "find the algebra rule for the pattern"

The rule can be found using two methods:

- 1. Comparing the diagram number with the number of shapes in it.
- 2. Comparing the number of shapes with the number of objects used to make each diagram.

Tables of values help with both methods



After looking at the first values of n = 1 and s = 4, the rule must be: s = 2n + 2

Using the general rule

The number of shapes/objects in a particular part of the pattern is found by substituting into the general rule.

How many Squares (s) are there in the 20^{th} pattern if s = 2n + 2?

when n = 20, $s = 2 \times 20 + 2 = 42$ squares.





Answers

Mathletics

	Words and symbols	Mixed simplifying concepts
1. 2.	a) The variable is b b) The variable is m c) The variable is k d) The variable is a 3+x= $x \div x = 1$ $12 \times g =$ $3 \times x + 6 =$	2. a $2 \times d \div 3$ b $(a+4) \div b$ c $(q-r) \div (9 \times q)$ d $l \times l \div (j-k)$ e $5 \times b \times b \div (a \times a + 2 \times b)$ f $7 \times x \times y \times z \div (x + 7 \times y)$
•••••		Phrases as algebraic expressions
3.	$14 - k \text{ if } x = 4$ $4 \times m \text{ if } m = 5$ $27 \div a \text{ if } a = 3$ $+ 37 \times z \text{ if } z = 3$	1. (a) $n+7$ (b) $9-n$ (c) $6 \times n+1 = 6n+1$ (d) $4 \times n = 4n$ (e) $\frac{n+2}{3}$ (f) n^2-6
4.	a $c = 8$ b $h = 12$ c $k = 18$ d $y = 6$	(a) $2(n-5)$ (b) $2n-8$ (c) $10 + \frac{n}{2}$ (c) $n(n+5)$
	Multiplication	2. a Correct b Incorrect c Correct
1.	a 14k b u c 5pr d 12jkl	d Incorrect e Incorrect f Correct
	e 18b ² f 12jkl	Incorrect Incorrect Incorrect
2.	a $4 \times p \times q$ b $4 \times a \times a$ c $3 \times m \times m \times n$	Correct
		Addition and subtraction
э.		1. (a) $10a$ (b) $8u$ (c) $5r$ (d) $-3g$
	Division	e $-2m$ f $-9x$ g $13y$ h $5p$
1.	a $\frac{2}{d}$ b $\frac{a}{c}$ c $\frac{5}{r+3}$ d $\frac{y+z}{z}$	2. (a) $25m + 9n$ (b) $14a + 11b$ (c) $16x + 24y$
2.	a $w \div 4$ b $c \div (3+a)$	d $6d - 5c$ e $18e + 2a$ f $-2g - 4h$
•••••	c $6 \div (3x+2)$ d $(x-y) \div (v+w)$	Grouping like terms
3.	a $a \div 3$ b $b \div 2c$	1. (a) $10a + 7b$ (b) $11p^2 + 22p$ (c) $-23m$
	c $3x \div 4y$ d $(m+n) \div 3p$	d $4y - 13x$ e $12p + 8q$ f $16a^2 + 4b - 3$
	Mixed simplifying concepts	2. a) $\frac{11y}{y+2x}$ b) $\frac{-p^2-5p}{12}$
1.	a) $\frac{5a}{4}$ b) $\frac{m}{4+n}$ c) $\frac{mn}{abc}$ d) $\frac{16p}{9q}$ e) $\frac{x^2}{y+2x}$ f) $\frac{d^2f}{11+ef}$	3. a) $\frac{4x - 3y}{7x - 2y}$ b) $\frac{8a + 6b}{5a^2}$



2

4

2

3

5

3

4

6

4

Escape from A	Algebra Island Puzzle		Tak	oles	of V	alu	es
3	x 2 $3x$	1.	a	v u	0		1
x 0 $2x$ x 0 $2x$ x x 0 x x x x 0 x	3x $6x$ $4xx 5x^2 0$		b	d c	0		1
$\begin{array}{c} 2 \\ 2 \\ x \\ 12x \\ 3x^2 \\ \end{array}$	$4x^{2} \qquad 3x^{2} \qquad x \qquad 6x$ $4x^{2} \qquad 8x \qquad 8x \qquad 6x$ $4x^{2} \qquad 2x \qquad 2x$ $1sland \qquad x \qquad 2x$	$\sim 2x$	C	h g	1		25
4x 2 $x8 8x$	$2x^{2}$ $2x^{2}$ $4x$ x^{2} $3x^{2}$ $4x^{2}$ $3x$		d	x y	2		4
2x - 6 - 3x $2x - 6 - 8x$		2.	a b	0 2	2 3	4	6
Bringing all the	e previous concepts together		a b	1	26	3 11	
 18 9 	b 3 d 2		a b	0	1 3	26	9
2. a 8	b 27		a b	0 3	1 5	2 7	<u> </u>
C 8	d 5	3.	a	x	0		1
3. a 54	b 30			У	5		6
c 4	d -9		b	т	0		1
4. a 7	b -6			n	0		4
c 60	d -6		C	р а	0		1
5. 2	6. 1		d	C	0		1



•	а	x	0	1	2	3	4
		У	5	6	7	8	9
	b	т	0	1	2	3	4
		п	0	4	8	12	16
	С	р	0	1	2	3	4
		q	-3	-2	-1	0	1
	d	С	0	1	2	5	6

-1

d -5

3

15

19

Mathletics



:

Number patterns

- a (i) Starting with one smiley face in the first diagram, 2 smiley faces are added to each diagram every time.
 - (ii) 1 , 3 , 5 , 7 , 9 , ...
 - (i) Starting with three arrows in the first diagram, 4 arrows are added to each diagram every time
 - (ii) 3 , 7 , 11 , 15 , 19 , ...
 - (i) Starting with 6 triangles to form the first diagram, 6 triangles are added to each diagram every time.

(ii) 6 , 12 , 18 , 24 , 30 , ...

2.	a (i)	Diagram number	1	2	3	4
		Number of hearts	2	5	8	11
(ii) 20						

```
b (i)Diagram number1234Number of hexagons381318
```

(ii) 33

- C (i)Diagram number1234Number of matchsticks371115
 - (ii) 27

Modelling Number Patterns





Using the general rule

1.	a 16 points	b 32 chickens
	c 25 shirts	d 12 vegetarion meals
2.	58	3. 39
4.	52	5. 70

6. 77











www.mathletics.com